

Measurement Uncertainty for Cd and P in Agricultural Top Soil

Ulrich Kurfürst

Evaluation:

- 1. Modelling approach** (single effect investigation, ISO/DIN "GUM")
- 2. Laboratory validation approach** (process replication, ISO/DIN 5725)



University of Applied Sciences Fulda

Andrea Knörle, Irina Maul, Kathrin Schneider,
Anita Strietzel, Arnd Wetzel, Nicole Wieser
Annette Niedling, Ulrich Kurfürst



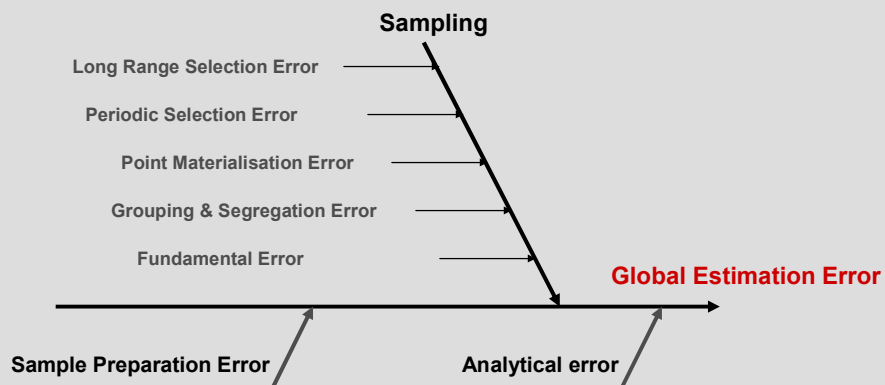
German Federal Agricultural Research Centre

Jürgen Fleckenstein
Ute Funder
Jutta Rogasik

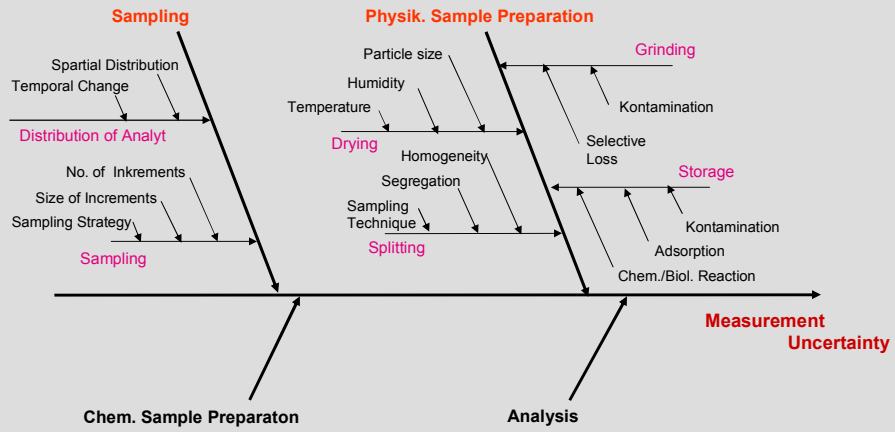
Modelling Approach

Classification of Effects in Sampling

("Sampling Theory" according to Gy)

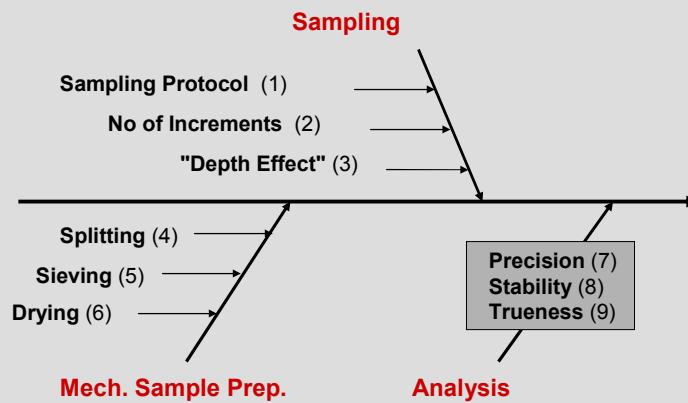


Effects in Soil Sampling



Modelling - Case Study

Tested Effects in Sampling, Sample Preparation and Analysis



Case Study



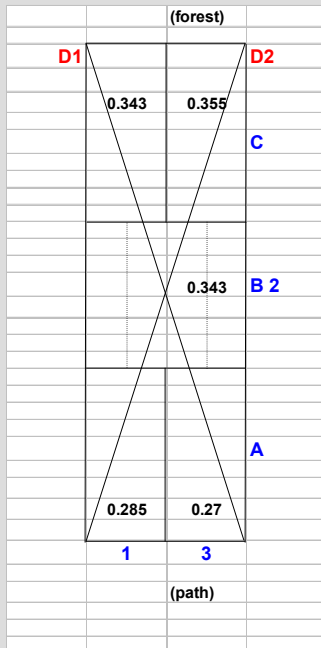
0.315 ha (143 m x 22 m)

Definition of measurand:

- Mass fraction of analyts of a soil body of 30 cm depth
- Sample material air dried, ground, and sieved to < 2 mm
- Sample produced according to a specified sampling protocol

Sampling Protocol (Strategy):

- Sampling scheme: Diagonal
- Auger sampling device
- 20 increments per ha



Modelling Approach

1. Sampling Strategy (system. effect)

Reference-Sampling:

5 composite samples from squares
A1, A3, B2, C1, C3; 18 incr. each

Difference **D1** and **D2**
(Cd)

$$\Delta x_{\text{Diag}} = 2.8 \%$$

("Typ B": U-Distribution)

$$u_{\text{Prot}} = \frac{\Delta x_{\text{Diag}} / 2}{\sqrt{2}}$$

$$u_{\text{Prot}} = 1.0 \%$$

Modelling Approach

2. Between Increment Locations (random effect)

9 increments on **square B**
(10 m x 10 m)

Increment	x (mg/kg)
1	0.364
2	0.411
3	0.468
4	0.413
5	0.370
6	0.376
7	0.389
8	0.376
9	0.464
$S_{ws} = 9.8 \%$	

(Cd)

Long range heterogeneity (betw. sqr): $S_{bs} = 12 \%$

Short range heterogeneity (within sqr): $S_{ws} = 9.8 \%$

$$S_{Incr} = \sqrt{S_{bs}^2 + S_{ws}^2} = 16 \%$$

("Typ A":
Normal Distribution)

$$u_{Incr} = \frac{S_{Incr}}{\sqrt{n_{Incr}}}$$

(each diagonal: $n_{Incr} = 9$)

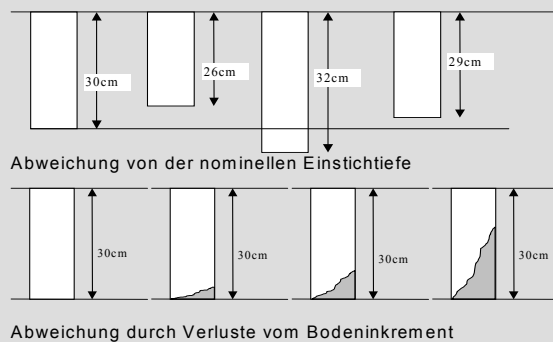
$$u_{Incr} = 5.4 \%$$



Modelling Approach

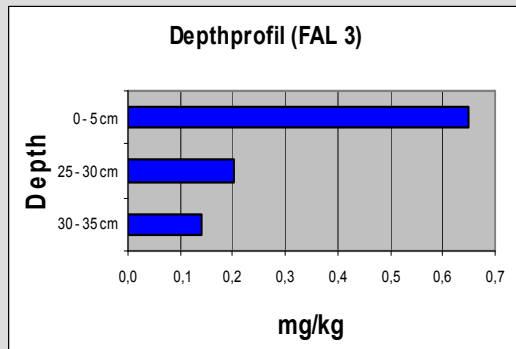
3. Depth Effect (1)

"Materialisation error"
(Delimitation and Extraction)



Modelling Approach

3. Depth Effect (2)
Analyt gradient in depth



Analytical values of cores
(mean of 5 cores):

(Cd)

(Ref. Depth)

- 5 cm: $c_- = 0.14$ mg/kg

(Ref. Depth)

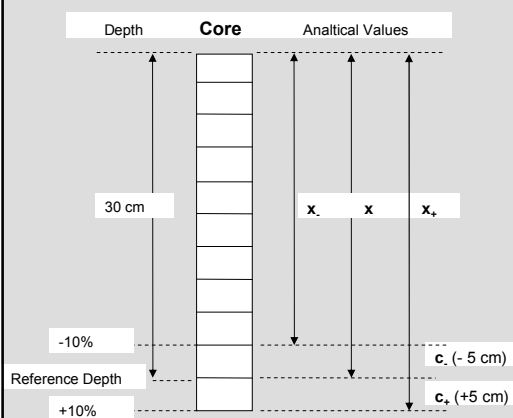
+ 5 cm: $c_+ = 0.10$ mg/kg

Modelling Approach

3. Depth Effect (3)

Transformation

Difference in depth \Rightarrow Difference in analyte content



Assumption:
max. deviation from ref. depth: $\pm 10\%$

("Type B":
Triangle
Distribution)

$$u_{\text{Depth}} = \frac{(x_+ - x_-)/2}{\sqrt{6}}$$

(Cd)

$u_{\text{Depth}} = 3.5\%$

Probenteilungsschema

Modelling Approach

4. Sample Splitting (1)

Test of duplicates from field samples (n = 18)

Method:
„pizza pieces“: 6 times to half mass

■ rejected
□ mixed again

Modelling Approach

4. Sample Splitting (2)

Distribution of standard deviations from 18 duplicate measurements

(„Typ A“:
Normal Distribution) $u_{Split} = s_{Split}$

(Cd)
Mean of standard deviations:
 $s_{Split} = 5.0\%$

$u_{Split} = 5.0\%$

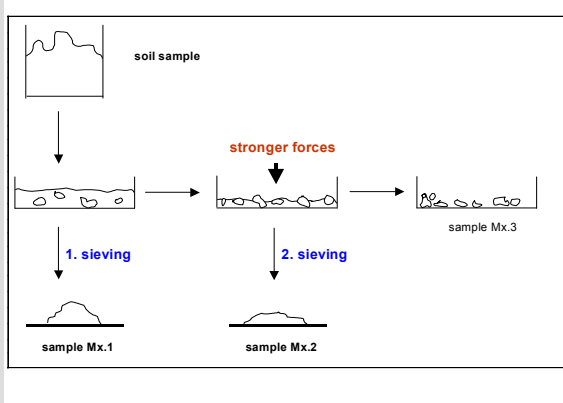
Modelling Approach

5. Sieving (particle size < 2mm)

Test of field samples (n = 6)

Max. difference Δ_{Siev} in analyte content of samples after 1. sieving (low force) and 2. sieving (stronger forces)

$$\Delta_{\text{Siev}} = |c_{1.s} - c_{2.s}|$$



(Cd) $\Delta_{\text{Siev}} = 6.6 \%$

("Type B" Rectangular distribution)

$$u_{\text{Siev}} = \frac{\Delta_{\text{Siev}} / 2}{\sqrt{3}}$$

$$u_{\text{Siev}} = 1.9 \%$$

Modelling Approach

6. Drying

Water content in prepared analytical samples

Reference*:

For a large number of sieved and *air dried* soil samples a water content was found between 1 - 3 %.

* R. Dahinden, A. Desaulles
Die Vergleichbarkeit von Schwermetallanalysen in Bodenproben von Dauerbeobachtungsflächen
Eidg. Forschungsanstalt für Agrarchemie und Umwelthygiene, Bern 1994

$$\Delta_{\text{Dry}} = 2.0 \%$$

("Type B" Rectangular distribution)

$$u_{\text{Dry}} = \frac{\Delta_{\text{Dry}} / 2}{\sqrt{3}}$$

$$u_{\text{Dry}} = 0.6 \%$$

Instrumental Analysis

Single laboratory validation data

Analytical Methode

Cd: Solid Sampling Zeeman-Graphitfurnace-AAS

	Uncertainty contribution	Evaluation	Standard-uncertainty
7.	Repeatability	Precision of test samples ("Typ A" Normal Distribution)	$U_{rw} = 3.6 \%$
8.	Long-term Stability	Control chart ("Typ A" Normal Distribution)	$U_{bias} = 2.7 \%$
9.	Trueness	Cert. Referencematerial (CRM) ("Typ B" Normal Distribution)	$U_{ref} = 2.7 \%$
<i>Combined analytical uncertainty</i>			$U_{anly} = 5.2 \%$

Uncertainty - Budget

Estimation of **Combined Measurement Uncertainty**

			Standarduncertainty	
			Cd	P
1.	Sampling protocol	Sampling	1.0 %	0.5 %
2.	Between locations		5.4 %	2.9 %
3.	Depth effect		3.5 %	3.7 %
4.	Splitting	Sample Prep.	5.0 %	2.5 %
5.	Sieving		1.9 %	2.4 %
6.	Drying		0.6 %	0.6 %
7.	Repeatability	Inst. Analysis	3.6 %	0.6 %
8.	Stability (lab. bias)		2.7 %	-
9.	Trueness		2.7 % ¹⁾	9.7 % ²⁾
Combined Uncertainty			9.1 %	11.3 %

¹⁾ Confidence interval of CRM BCR 280

²⁾ S_R from an Inter-Laboratory Comparison

Laboratory Validation Approach

Six independent sampling processes

- Sampling under reproducibility conditions
- Analysis under repeatability conditions

Sampler	Diagonal	Cd (mg/kg)
1	D1	0.314
2	D1	0.304
3	D1	0.345
4	D2	0.313
5	D2	0.313
6	D2	0.350

$$\bar{x} = 0.323$$

$$s_R = 6.0 \%$$

Samp = R

Measurement Uncertainty
(including the analytical components u_{bias} , u_{ref}):

$$u_{\text{meas}} = 8.0 \%$$

Case Study

Measurement Uncertainty for Cd and P in Agricultural Top Soil

Comparison of Methods

Expanded Uncertainty :

$$U_{\text{meas}} = k \times u_{\text{meas}}$$

	Laboratory Validation	Modelling
Cd	19 % ¹⁾	18 % ³⁾
P	26 % ²⁾	23 % ⁴⁾

Faktor k for approx. 95% coverage:
¹⁾ $k = 2.4$ ($df_{\text{eff}} = 7$) ³⁾ $k = 2.0$ ($df_{\text{eff}} > 30$)
²⁾ $k = 2.1$ ($df_{\text{eff}} = 20$) ⁴⁾ $k = 2.0$ ($df_{\text{eff}} > 30$)

Ulrich Kurfürst et al.:

**Repräsentanz von Probennahmeverfahren auf Ackerflächen
- eine Fallstudie zur Ermittlung der Messunsicherheit für
Cadmium und Phosphor
(Endbericht)**

**Representativity of Sampling on Arable Land
- a Case Study of Evaluation of Uncertainty in Measurement for
Cadmium and Phosphorus
(Final Report)**

**WWW. [HS-Fulda.de/fileadmin/Fachbereich_OE/
Download/Profs/UK/Bericht_PronAck_06.pdf](http://HS-Fulda.de/fileadmin/Fachbereich_OE/Download/Profs/UK/Bericht_PronAck_06.pdf)**